

# Nowcasting from Urban to Continental Scale: An Illustration of Scaling Characteristics

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# Overview

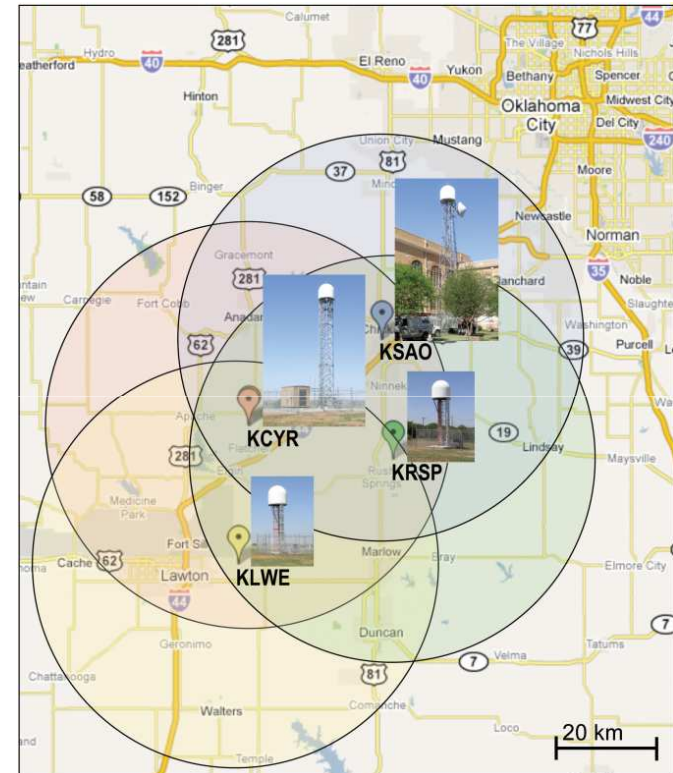


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# Introduction



- The Collaborative Adaptive Sensing of the Atmosphere (CASA) radar nowcasting system was developed to provide highly localized urban-scale quantitative precipitation forecasts using networked X-band radars
- This presentation discusses
  - Scalability of the CASA nowcasting model to continental-scale
  - Model parameterization relative to the space-time characteristics of precipitation



# Methodology — Motion Estimation



- The Dynamic Adaptive Radar Tracking of Storms (DARTS) model is based on a discrete representation **(2)** of the general continuity equation **(1)** formulated as a linear system **(3)** in Fourier space

$$\frac{\partial}{\partial t} F(x, y, t) = -U(x, y) \frac{\partial}{\partial x} F(x, y, t) - V(x, y) \frac{\partial}{\partial y} F(x, y, t) + S(x, y, t) \quad (1)$$

$$k_t F_{\text{DFT}}(k_x, k_y, k_t) =$$
$$- \left[ \frac{1}{N_x N_y} \right] \sum_{k'_x=N_x^-}^{N_x^+} \sum_{k'_y=N_y^-}^{N_y^+} \left[ \frac{U_{\text{DFT}}(k'_x, k'_y)}{T_x / T_t} \right] (k_x - k'_x) F_{\text{DFT}}(k_x - k'_x, k_y - k'_y, k_t)$$

$$- \left[ \frac{1}{N_x N_y} \right] \sum_{k'_x=N_x^-}^{N_x^+} \sum_{k'_y=N_y^-}^{N_y^+} \left[ \frac{V_{\text{DFT}}(k'_x, k'_y)}{T_y / T_t} \right] (k_y - k'_y) F_{\text{DFT}}(k_x - k'_x, k_y - k'_y, k_t)$$

$$- \left( \frac{i}{2\pi} \right) \left[ T_t S_{\text{DFT}}(k_x, k_y, k_t) \right] \quad (2)$$

$$\mathbf{y} = \mathbf{H}\mathbf{x} \quad \leftarrow \text{Increased smoothness implies smaller model size} \quad (3)$$



# Methodology — Advection

- An analytical based on sinc kernel interpolation (spatial domain)
- Used as a tool to characterize scales of precipitation

$$F_{kl}(t + \delta_t) = F_{kl}(t) - \left\{ \frac{U_{kl}}{\Delta x} \cdot [\mathbf{A}\mathbf{F}(t)]_{kl} + \frac{V_{kl}}{\Delta y} [\mathbf{F}(t)\mathbf{Z}]_{kl} \right\} \delta_t$$

where,

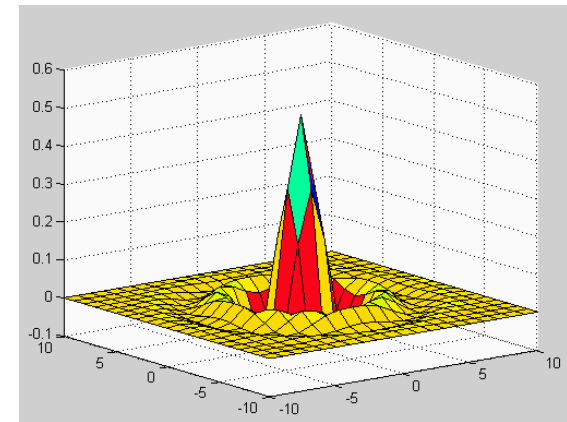
$$\mathbf{A} \equiv [A_{km}] = [\text{Dsinc}(k - m)]$$

$$\mathbf{Z} \equiv [Z_{nl}] = [\text{Dsinc}(n - l)]$$

$$\mathbf{F}(t) \equiv [F_{ml}(t)] \text{ or } \mathbf{F}(t) \equiv [F_{kn}(t)]$$

$$\text{Dsinc}(x) \equiv \frac{d}{dx} \text{sinc}(x) = \begin{cases} \frac{1}{x} [\cos(\pi x) - \text{sinc}(x)] & x \neq 0 \\ 0 & x = 0 \end{cases}$$

Controls resolution (step size)



# Methodology — Advection

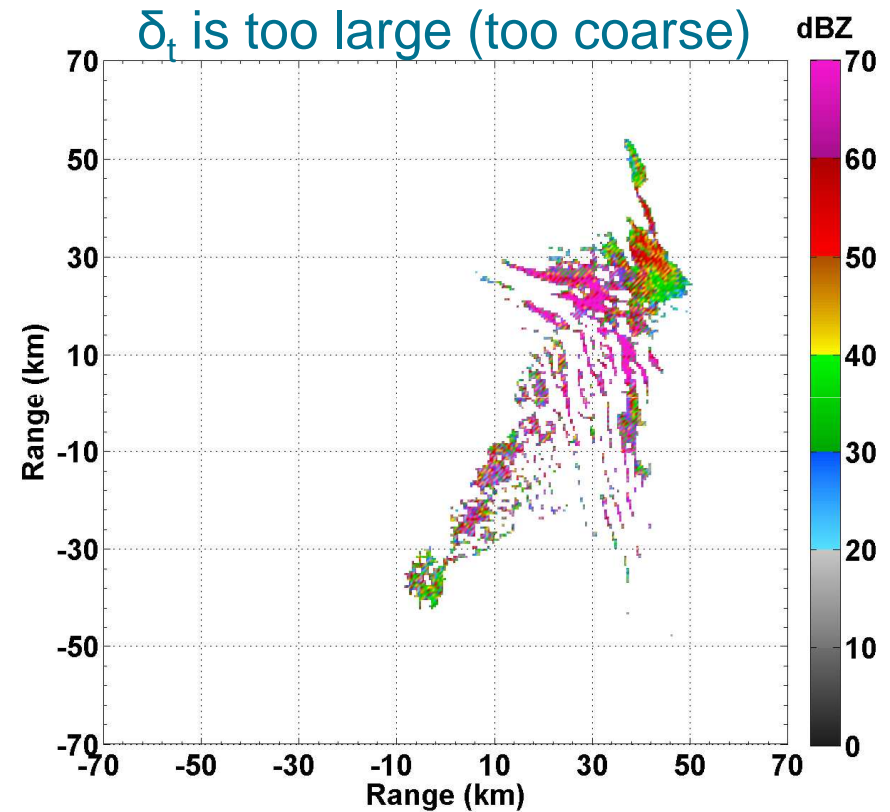
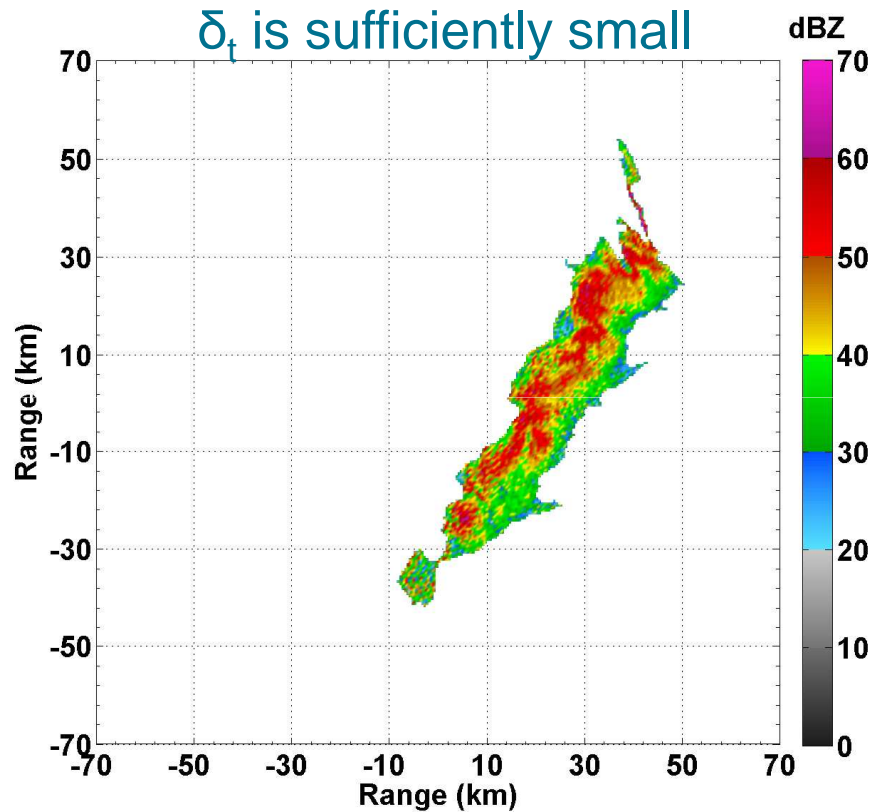


Illustration advection instability used as the reference for parameterization

# Methodology — Advection

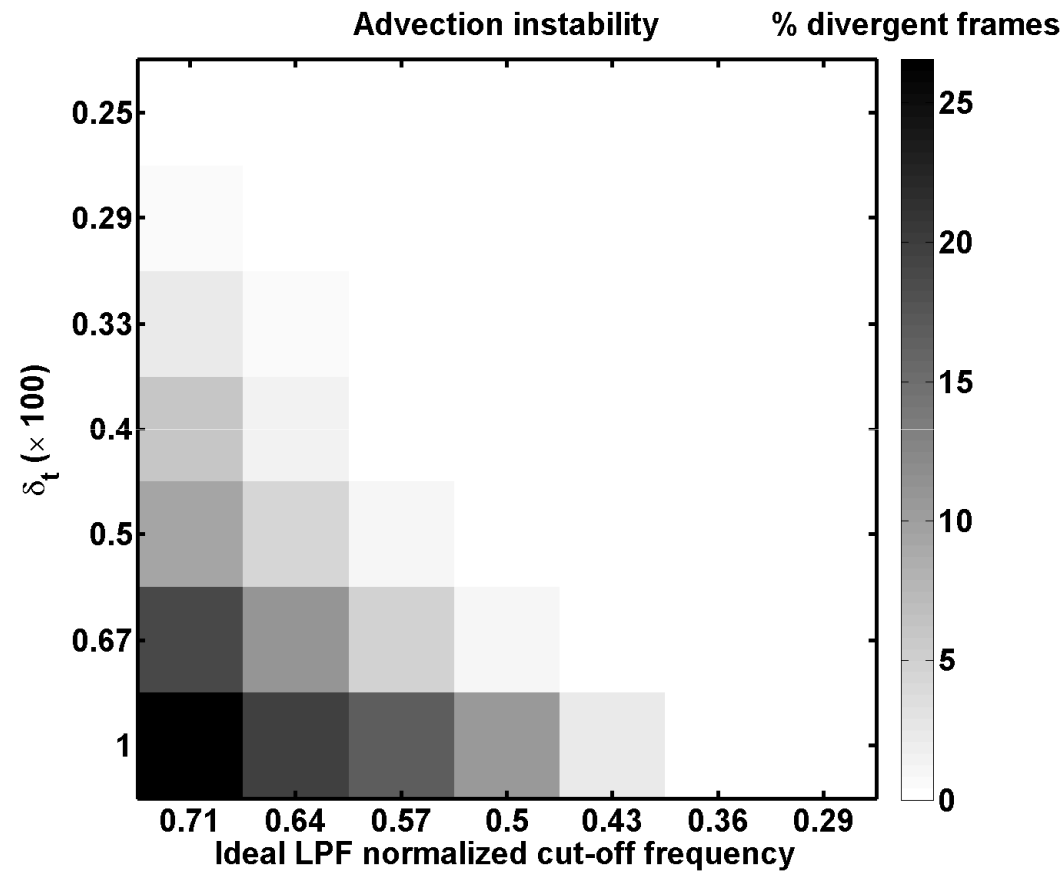


Illustration of advection parameterization vs. advection stability

# Experimental Description

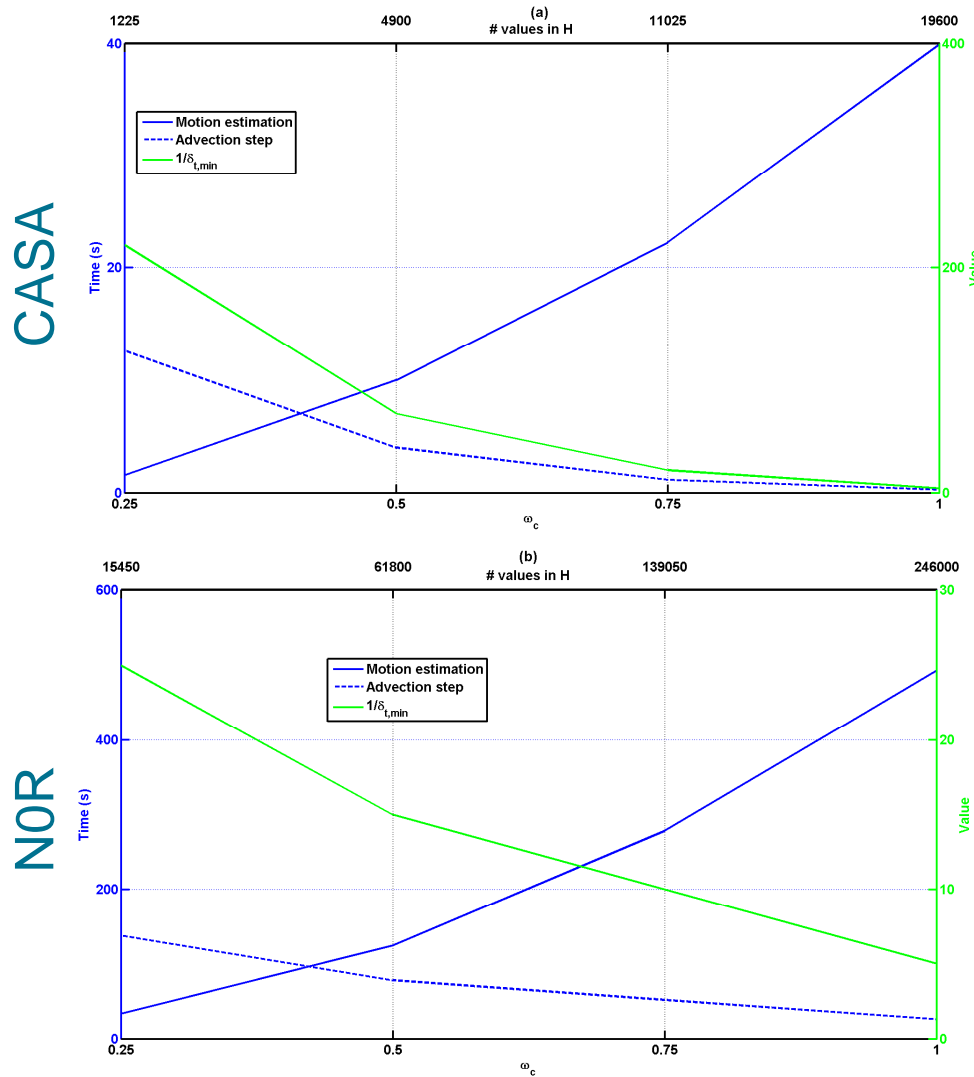


- Considered CASA and NEXRAD (N0R) national composite data
- Two experiments were performed to assess the characteristics of the nowcasting model relative to the size of the data and precipitation scales being tracked
  - Fixed size of input radar data fields while varying the normalized cut-off frequency of the LPF represented by the dimensions of **H**
    - Grid spacing: 0.5 km (CASA); 4 km (N0R)
    - LPF cut-off frequency: 0.25 to 1.0 in steps of 0.25
  - Varied sizes of data fields/grid spacing and fixed the cutoff frequency of the LPF
    - Grid spacing: 0.5, 1, 2, 4 km (CASA); 4, 6, 8, 12 km (N0R)
    - LPF cut-off frequency: 0.20
- Considered maximum value (coarsest) of  $\delta_t$  to achieve stability





# Results



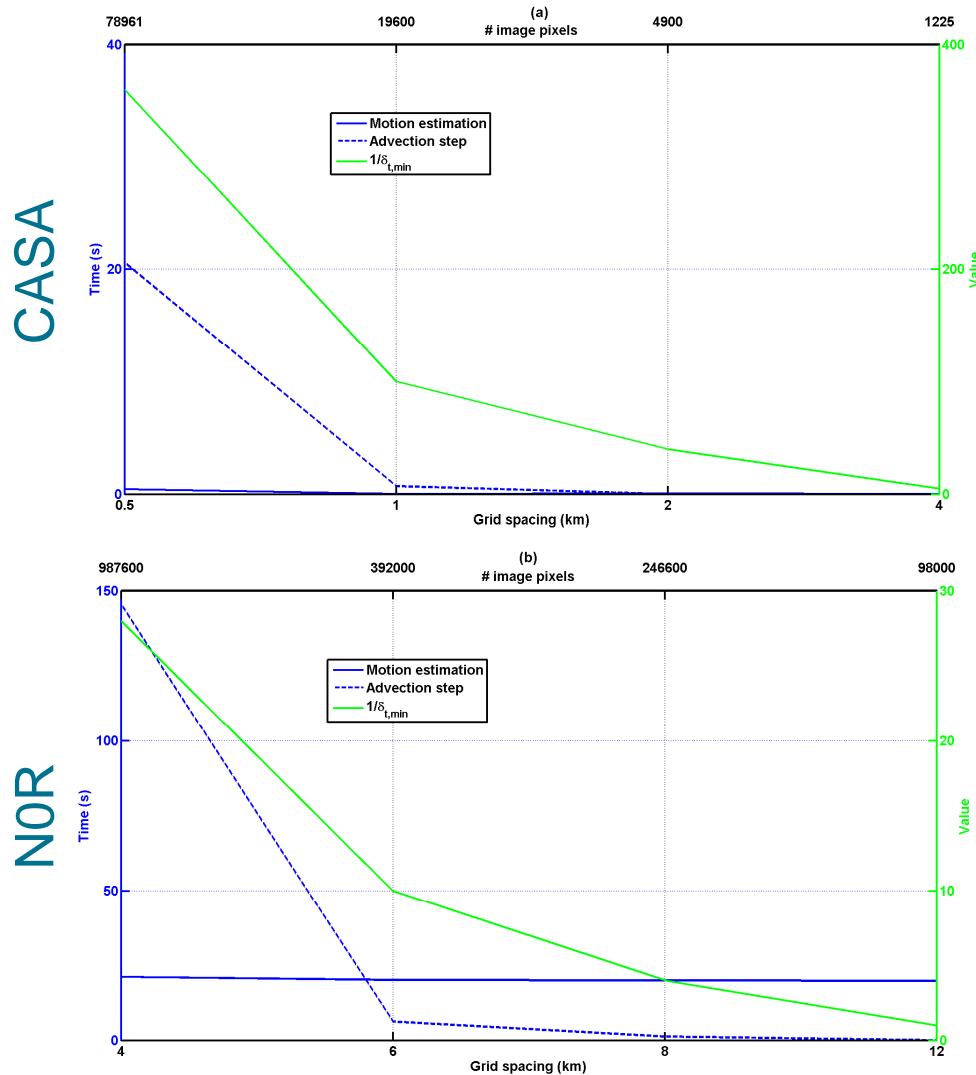
Runtime (blue) and advection parameter characteristics (green) considering a fixed data size and varying size of the model design matrix  $\mathbf{H}$  for (a) CASA and (b) NOR data



**A smaller advection step size must be used when estimating motion of larger precipitation scales (faster propagation than smaller scales)**



# Results



Runtime (blue) and advection parameter characteristics (green) considering a fixed size of the model design matrix  $\mathbf{H}$  and varying data size for (a) CASA and (b) NOR



**A larger advection step size can be used with data that has been smoothed to lower resolutions**

# Summary and Conclusions



- Illustrated the scalability of the CASA nowcasting system to continental-scale
  - CASA (0.5 km; 140 km × 140 km) vs. NEXRAD composite (4 km; 4800 km × 3200 km)
- Discussed model parameterization relative to the space-time characteristics of precipitation
  - LPF cut-off frequency (motion estimation model)
  - Step size (advection model)
- Quantified the relative differences in propagation speed of large- and small-scale precipitation features using the model parameters
  - Larger-scale features propagate faster thus requiring a finer advection step (smaller  $\delta_t$ )

# Summary and Conclusions



- Showed the nonlinear scaling behavior of the nowcasting model
  - Suggests the motion estimation model design matrix  $\mathbf{H}$  should be truncated to facilitate reasonable computation times and thus the tracking of larger scales shown to be more representative of precipitation pattern envelope motion
  - An alternate advection scheme should be considered when using data projected onto large grids, with size dependent on the application requirements



# Questions?